

# A Novel Regression Method for Software Defect Prediction with Kernel Methods

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Abstract: In this paper, we propose a novel method based on SVM to predict the number of defects in the files or classes of a software system. To model the relationship between source code similarity and defectiveness, we use SVM with a precomputed kernel matrix. Each value in the kernel matrix shows how much similarity exists between the files or classes of the software system tested. The experiments on 10 Promise datasets indicate that SVM with a precomputed kernel performs as good as the SVM with the usual linear or RBF kernels in terms of the root mean square error (RMSE). The method proposed is also comparable with other regression methods like linear regression and IBK. The results of this study suggest that source code similarity is a good means of predicting the number of defects in software modules. Based on the results of our analysis, the developers can focus on more defective modules rather than on less or non defective ones during testing activities.

## 1 INTRODUCTION

Predicting the number of defects or the extent of defectiveness in the software modules is a very crucial issue. With a successful prediction process, developers can spend their time more effectively as they would deal with the most defective parts of the software system rather than reinspecting the defect free modules. As a result of a well-advised testing, the probability of fixing the residual defects would increase and more qualified software products would be delivered to the end users. Moreover, since more defects would be fixed during the testing phase, the maintenance costs will decrease and this will lead to a decrease in the total cost of the project itself.

Software metrics are used in defect prediction studies and there are different types of metrics used in the literature like McCabe (McCabe, 1976) and Halstead metrics (Halstead, 1977). Menzies et al. show that how the code metrics are used to build predictors is much more important than which particular metrics are used. Furthermore, they also suggest that McCabe and Halstead metrics are intra module metrics and new metrics showing the interactions among different modules (inter module metrics) shall be used that yield better defect predictors (Menzies et al., 2007). Similarly, Zimmermann and Nagappan suggest that, understanding of the dependencies that exist between

different pieces of the code is very important to predict the defect-proneness of software systems (Zimmermann and Nagappan, 2009).

Machine learning based techniques are used frequently in defect prediction studies. Random forest (Kaur and Malhotra, 2008), linear discriminant analysis (Munson and Khoshgoftaar, 1992), artificial neural networks (Kaur et al., 2009), *K*-nearest neighbour (Boetticher, 2005), Bayesian networks (Pai and Dugan, 2007) and support vector machine based classifiers (Lessmann et al., 2008) (Hu et al., 2009) (Xing et al., 2005) (Gondra, 2008) are some of the machine learning algorithms that are used in the fault prediction literature.

In this paper, we propose a novel method to predict the number of defects in the software modules by focusing on the source code similarity. We generate a precomputed kernel matrix that shows the similarity among different classes or modules of the software system and use this matrix as a precomputed kernel for SVM to predict the number of defects or the extent of defectiveness. To extract the similarities among different classes or modules we use the plagiarism tool MOSS (Aiken, 1997).

This paper is organized as follows: In Section 2, we give a background on kernel machines. In Section 3, we present a brief review of previous work on kernel methods and software defect prediction using

kernel machines. We explain our proposed method in Section 4 and give the experiments and results in Section 5 before we conclude in Section 6.

## 2 KERNEL MACHINES

### 2.1 Support Vector Machines

Let's assume that we have a training set where  $y^t$ 's are output values corresponding to each  $\mathbf{x}^t$  input vector.

In SVM regression proposed by Vapnik et al. (Cortes and Vapnik, 1995) the goal is to find a function  $g(\mathbf{x})$  that has at most  $\varepsilon$  deviation from the actually obtained target  $y^t$  values for all of the training data, and at the same time is as flat as possible. It means that the error  $e$  introduced by the function  $g(\mathbf{x})$  must be less than  $\varepsilon$  for all possible  $\mathbf{x}$  inputs. If the function  $g(\mathbf{x})$  is defined as:

$$g(\mathbf{x}^t) = \mathbf{w}^T \mathbf{x}^t + b \quad (1)$$

the  $\varepsilon$ -sensitive error function can be defined as:

$$e_\varepsilon(y^t, g(\mathbf{x}^t)) = \begin{cases} 0 & \text{if } |y^t - g(\mathbf{x}^t)| < \varepsilon \\ |y^t - g(\mathbf{x}^t)| - \varepsilon & \text{otherwise} \end{cases} \quad (2)$$

where for the function to be flat,  $\mathbf{w}$  should be small. To ensure a small  $\mathbf{w}$ , we can minimize  $\|\mathbf{w}\|^2 = (\mathbf{w}^T \mathbf{w})$ . Then, we can write this problem as a convex optimization problem of:

$$\begin{aligned} & \text{Minimize } \frac{1}{2} \|\mathbf{w}\|^2 & (3) \\ \text{s. t. } & \begin{cases} y^t - (\mathbf{w}^T \mathbf{x}^t + b) \leq \varepsilon \\ \mathbf{w}^T \mathbf{x}^t + b - y^t \leq \varepsilon \end{cases} \end{aligned}$$

To control the sensitivity of SVM and tolerate possible outliers, slack variables ( $\xi_+, \xi_-$ ) are introduced. Then the problem changes slightly and becomes an optimization problem of

$$\begin{aligned} & \text{Minimize } \frac{1}{2} \|\mathbf{w}\|^2 + C \sum_t (\xi_+^t + \xi_-^t) & (4) \\ \text{s. t. } & \begin{cases} y^t - (\mathbf{w}^T \mathbf{x}^t + b) \leq \varepsilon + \xi_+^t \\ \mathbf{w}^T \mathbf{x}^t + b - y^t \leq \varepsilon + \xi_-^t \\ \xi_+^t, \xi_-^t \geq 0 \end{cases} \end{aligned}$$

where the constant  $C > 0$  determines the trade-off between the flatness of  $g(\mathbf{x})$  and the amount up to which deviations larger than  $\varepsilon$  are tolerated and two types of

slack variables ( $\xi_+, \xi_-$ ) are used, for positive and negative deviations, to keep them positive. This formulation also corresponds to the  $\varepsilon$ -sensitive error function given in Equation 2. The Lagrangian is:

$$\begin{aligned} L_p = & \frac{1}{2} \|\mathbf{w}\|^2 + C \sum_t (\xi_+^t + \xi_-^t) \\ & - \sum_t \alpha_+^t (\varepsilon + \xi_+^t - y^t + \mathbf{w}^T \mathbf{x}^t + b) \\ & - \sum_t \alpha_-^t (\varepsilon + \xi_-^t + y^t - \mathbf{w}^T \mathbf{x}^t - b) \\ & - \sum_t (\mu_+^t \xi_+^t + \mu_-^t \xi_-^t) \end{aligned} \quad (5)$$

Taking the partial derivatives of the Lagrangian and substituting the results we get the dual:

$$\begin{aligned} L_d = & -\frac{1}{2} \sum_t \sum_s (\alpha_+^t - \alpha_-^t) (\alpha_+^s - \alpha_-^s) (\mathbf{x}^t)^T \mathbf{x}^s \\ & - \varepsilon \sum_t (\alpha_+^t + \alpha_-^t) - \sum_t y^t (\alpha_+^t - \alpha_-^t) \end{aligned} \quad (6)$$

subject to

$$0 \leq \alpha_+^t \leq C, 0 \leq \alpha_-^t \leq C, \sum_t (\alpha_+^t - \alpha_-^t) = 0$$

When we solve this, we see that all instances that fall in the regression tube have  $\alpha_+^t = \alpha_-^t = 0$  where these are instances that are fitted with enough precision. On the other hand, the support vectors are either  $\alpha_+^t > 0$  or  $\alpha_-^t > 0$  and are of two types. They can either be the instances on the boundary of the regression tube and can be used to calculate  $b$  in  $g(\mathbf{x})$ . Instances that fall outside of the regression tube are of the second type and we do not have a good fit for them ( $\alpha_+^t = C$ ).

The dot product  $(\mathbf{x}^t)^T \mathbf{x}^s$  in Equation 6 can be replaced with a suitable kernel function  $K(\mathbf{x}^t, \mathbf{x}^s)$  to have a nonlinear fit. For example, when we use a polynomial kernel we can fit to a polynomial or when we use a Gaussian kernel we can have a nonparametric smoothing model.

## 3 PREVIOUS WORK

Gondra (Gondra, 2008) compares the performance of Artificial Neural Network (ANN) with SVM and concludes that SVM is a better defect prediction technique when compared with ANN since its accuracy is higher. Elish and Elish (Elish and Elish, 2008) compare the performance of SVM with eight statistical and machine learning methods in terms of accuracy, precision, recall and the F-measure and suggest that the performance of SVM is better than or at least competitive with other statistical and machine learning

methods. Arisholm et al. (Arisholm et al., 2007) compare the performance of SVM with other techniques like C4.5, neural networks, and logistic regression in terms of precision, recall, and the AUC. Although they suggest that C4.5 classification tree method performs better than other techniques in general, the results are comparable in terms of the AUC where the AUC for SVM is 83.7% which is better than the AUC value of the six out of eight methods tested. Shin et al. (Shin et al., 2007) show that defect proneness prediction is possible even with just line of code ( $L$ ) and cyclomatic complexity ( $V$ ) metrics using radial basis function with Gaussian kernel. Hu et al. (Hu et al., 2009) show that SVM is more successful than ANN in terms of accuracy to predict software risks.

## 4 PROPOSED METHOD

We propose to use SVM with a precomputed kernel matrix to predict the number of defects in classes or files of the software systems. To generate the precomputed kernel matrix, we use the MOSS (Aiken, 1997) plagiarism detection tool which uses finger print approaches rather than considering lexical similarities only. We believe that defective code pieces have similar attributes in common and this similarity can be used to predict defectiveness.

Imagine a software system that has  $N$  files where a file is represented as  $f_i$ . Then the precomputed kernel matrix we generate from MOSS is represented as:

$$K = \begin{bmatrix} K(f_1, f_1) & K(f_1, f_2) & \dots & K(f_1, f_N) \\ K(f_2, f_1) & K(f_2, f_2) & \dots & K(f_2, f_N) \\ \dots & \dots & \dots & \dots \\ K(f_N, f_1) & K(f_N, f_2) & \dots & K(f_N, f_N) \end{bmatrix} \quad (7)$$

where  $K(f_i, f_j)$  shows the similarity between files  $f_i$  and  $f_j$ .

The kernel matrices generated for our data sets are valid kernels since they satisfy the positive semi-definiteness property. If any symmetric but non semi-positive matrix is not a valid kernel, there are some alternative ways of converting it to a valid kernel (Wu et al., 2005). Furthermore, we normalize the precomputed kernels to their unit norm, since normalization may effect the generalization ability and may result in a smaller range for  $C$ .

MOSS (Measure Of Software Similarity) is a tool developed by Alex Aiken and hosted by Stanford University (Aiken, 1997). MOSS uses robust winnowing algorithm, which is more efficient and scalable since it selects fewer finger prints for the same quality of results than previous algorithms tried (Schleimer et al., 2003). While generating a similarity output

Table 1: The 10 data sets used in the experiments.

Data Set	Version	Num. of Instances
Camel	1.0	339
Tomcat	6.0	858
Poi	3.0	442
Xalan	2.5	803
JEdit	4.0	306
Velocity	1.5	214
Ant	1.7	745
Lucene	2.4	340
Synapse	1.2	256
Ivy	2.0	352

with MOSS, its parameters  $m$  and  $n$  need to be tuned carefully.  $m$  represents the maximum number of times a given passage may appear before it is ignored, so we select  $m$  very large (1,000,000) not to ignore any similarity. Furthermore,  $n$  represents the maximum number of similarities to include in the results and we select it as 5,000 that is large enough to take into account all meaningful similarities for our case.

## 5 EXPERIMENTS AND RESULTS

### 5.1 Experiment Design

We use Weka (Hall et al., 2009) to compare the performance of our proposed kernel method (PCK-SVM) with linear, RBF kernels and other defect prediction methods LR and IBK. In each experiment,  $5 \times 2$  fold cross-validation is used and all the necessary parameters of SVM ( $C$ ,  $\epsilon$ , and  $\gamma$ ) are tuned. Furthermore, we compare all techniques in terms of the Root Mean Square Error (RMSE) metric. We select 10 data sets from the Promise data repository (Boetticher et al., 2007) (See Table 1) that are open source and have enough entries in their defect files to be able to apply  $5 \times 2$  cross validation.

We define the major steps followed for each experiment below:

1. First we choose appropriate open source data sets from Promise data repository. (See Table 1).
2. We give the source code of the data set to MOSS and extract the similarities that exist among the classes of the data set we chose.
3. We convert the MOSS similarity output to a pre-computed kernel matrix that shows similarities among the classes (or files).
4. We create a new defect file from the Promise data defect file that includes only the file names and

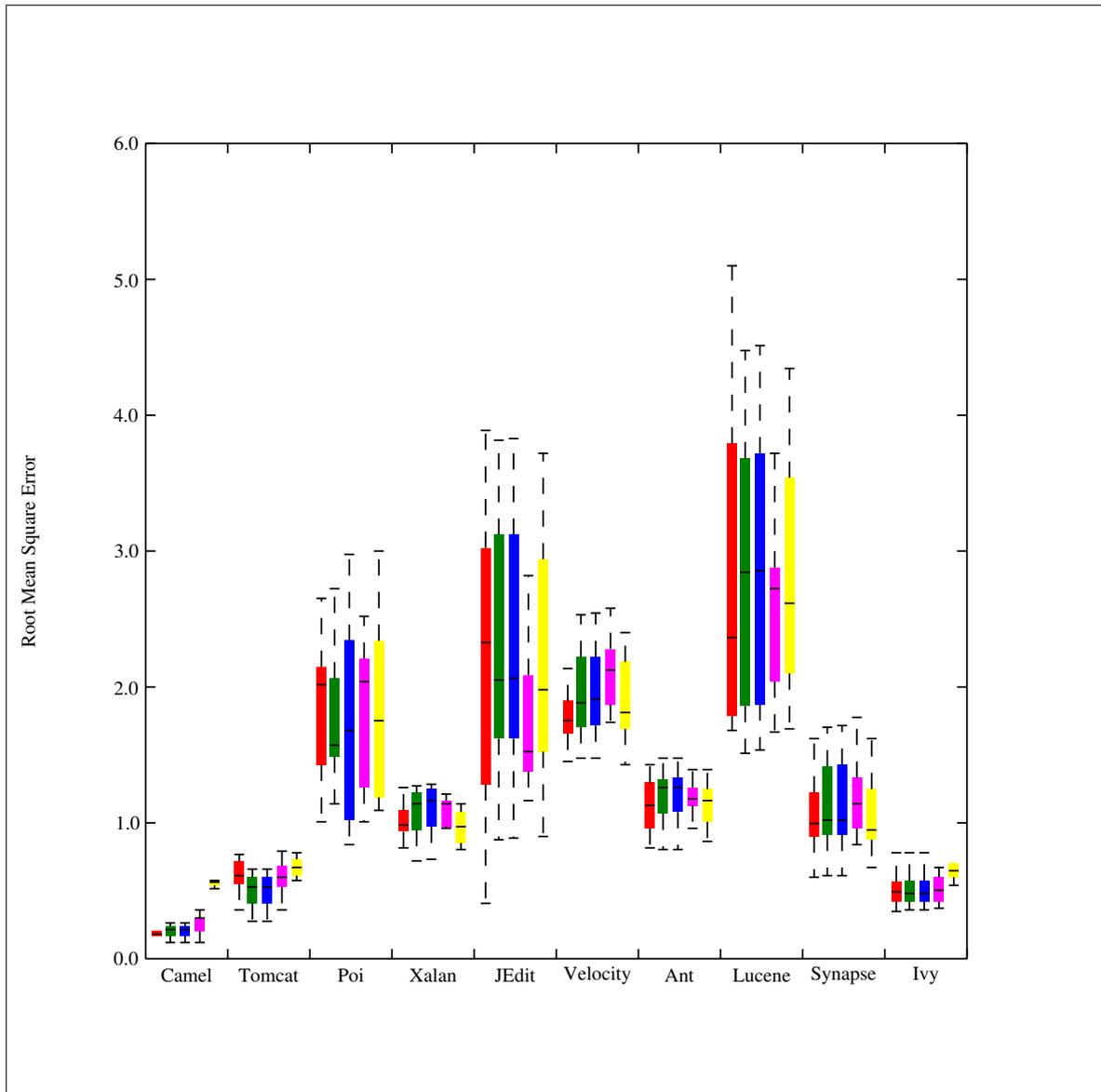


Figure 1: Box plots of RMSE of PCK-SVM, L-SVM, RBF-SVM, IBK, and LR for 10 datasets.

Table 2: A comparison of PCK-SVM with L-SVM, RBF-SVM, LR, and IBK algorithms. The first values in each cell show the number of cases where PCK-SVM is better than the algorithm in the column. The second values in each cell give the number of cases where PCK-SVM is worse than the algorithm in the column. The third values in each cell, represent the number of cases where there is a tie.

	L-SVM	RBF-SVM	LR	IBK
PCK-SVM	6, 3, 1	6, 2, 2	8, 2, 0	6, 4, 0

the number of bugs.

- To measure the performance of the proposed method (PCK-SVM), the defect file generated in step 4 and the precomputed kernel found in step 3 are given as inputs to SVM regression (SMOReg)

in Weka with  $5 \times 2$  cross validation.

- To measure the performance of other kernels (L-SVM and RBF-SVM) and existing defect prediction methods (LR and IBK), the original defect data file from Promise data repository is used.

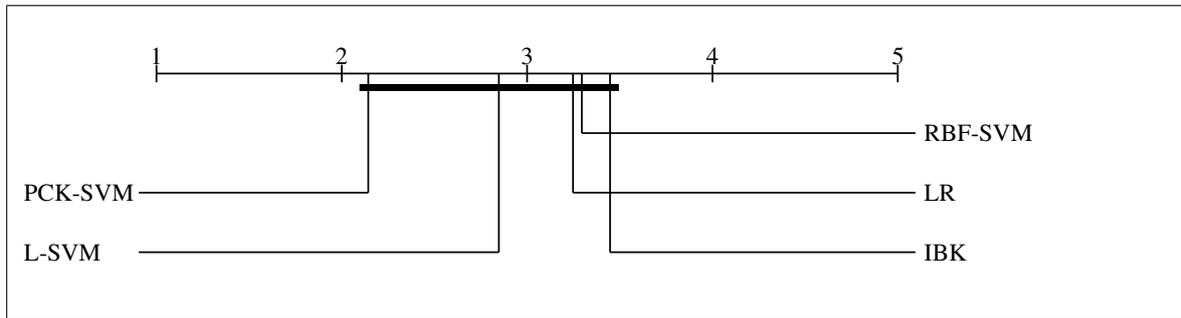


Figure 2: The mean ranks of the PCK-SVM, L-SVM, RBF-SVM, IBK, and LR.

The results of all methods are compared using the Root Mean Square Error (RMSE) where a smaller error interpreted as a better fit for regression.

## 5.2 Results

We compare the performance of precalculated kernel based SVM (PCK-SVM) with linear kernel (L-SVM), RBF kernel (RBF-SVM), linear regression (LR), and IBK algorithms. We see that PCK-SVM achieves a smaller RMSE compared to L-SVM in 6 of 10 experiments, whereas it is worse in 3 experiments and in 1 experiment there is no difference. Similarly, it generates better RMSE in 6 experiments, whereas it is worse in only 2 experiments when compared to RBF-SVM. When we compare the results with existing techniques, we observe that PCK-SVM is better in 6 experiments but worse in 4 experiments when compared with IBK. Similarly, for LR, it is better numerically in 8 experiments and it is worse in only 2 experiments (See Table 2).

We apply the Nemenyi post hoc test (in 95 % confidence interval) to detect if the performance of PCK-SVM differs significantly from other kernels and defect prediction techniques (Demšar, 2006). The result of the test is shown in Figure 2. We observe that although PCK-SVM is the best algorithm, it is still on the same block with other algorithms and there is no significant difference among the mean ranks of the tested algorithms. However, since it is on the border of the critical difference block, if more algorithms are tested on the same data sets, it could be possible to visualize the difference of PCK-SVM better.

We also check the statistical significance of the results, by applying unpaired *t*-test (in 95 % confidence interval) to the results obtained for PCK-SVM, L-SVM, RBF-SVM, LR, and IBK methods. We see that, although the mean ranks of the techniques are not different statistically, we observe significant differences for some data sets. For example, the performance of PCK-SVM is better than LR, for Camel and

Ivy data sets with a p-value of 0.0 and 0.004 respectively (See Figure 1). As a conclusion, we see that PCK-SVM is comparable not only with existing linear and RBF kernels, but also with existing defect prediction techniques in the literature i.e. LR and IBK.

## 6 CONCLUSIONS AND FUTURE WORK

In this paper, we propose a new kernel method to predict the number of defects in the software modules (classes or files). The proposed method is based on a precomputed kernel matrix which is based on the similarities among the modules of the software system. We compare our novel kernel method with existing kernels in the literature (linear and RBF kernels) and show that it achieves comparable results. Furthermore, the proposed defect prediction method is also comparable with some existing famous defect prediction methods in the literature i.e. linear regression and IBK.

The main contributions of this research are:

- We propose a novel kernel method to predict the number of defects in the software modules.
- Prior to test phase or maintenance, developers can use the proposed method to easily predict the most defective modules in the software system and focus on them primarily rather than testing each and every module in the system. This can decrease the testing effort and the total project cost automatically.

As a future work, we plan to refine our research and use graph based clone detection techniques which are able to detect functional similarities and are more successful compared to the token based techniques in extracting semantic similarities (Roy et al., 2009). We believe that when semantic similarity is included, the RMSE of the proposed prediction method would be lower.

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